

Semantic types of an anchored addition and subtraction¹

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The poster will be split into six main sections: illustrations of fundamental terms; definitions; tasks; student's solutions; examples; didactic applications of theoretical ideas.

As a continuation of G. H. Littler's poster about semantic types of numbers (Ad = address, St = state, Co = comparison, Ch = change) the most frequent semantic types of the addition and the subtraction are discussed:

Type	E x a m p l e
St + Ch	I had 10 Kč. I found 5 Kč. How many Kč do I have now?
St - Ch	I had 10 Kč. I lost 5 Kč. How many Kč do I have now?
St + Co	Ed is 124 cm high, Eva is 3 cm higher. How tall is Eva?
St - Co	Ed is 124 cm high, Eva is 3 cm lower. How tall is Eva?
St + St	Here you see 5 girls and 4 boys. How many children are here?
St - St	Here are 9 children. 5 of them are girls. How many boys are here?

We asked pupils to indicate the semantic inverse of these cases. There were no problems with the issues $St \pm Ch$ and $St \pm Co$, since words *to lose* and *to find* as well as *higher* and *lower* have been identified as opposite by all pupils. However the issue $St \pm St$ was a difficulty. The most frequent opposite to *put together* was identified as *to part the whole* or *do not touch it*. And the most frequent opposite to *take the complement* was identified either *take the whole* or *take the starting part* or *do not take the complement*.

Consequence. To be prepared to grasp the idea of subtraction a child has to be familiar with cases $St + Ch$ and $St + Co$. If the majority of his/her semantic experiences with the addition is of the type $St + St$ a child is not well prepared to understand subtraction.

Types $Ad \pm Co$ (I live on the 5th floor and Fred lives 2 floors above/below. On what floor does Fred live?) or $Ad \pm Ch$ (Our family moved from the 5th floor 2 floors up/ down. On what floor do we live now?) are of the same difficulty as $St \pm Ch$ and $St \pm Co$. A child must to meet these cases as well.

More demanding are types $Co \pm Co$ and $Ch \pm Ch$ (Ann is 2 years older than Bert and he is 1 year older than Cindy. How many years is Cindy older than Ann?) Here some children ask for the starting state (the age of Ann). Even more demanding are the cases $Co \pm Ch$ and $Ch \pm Co$ (During the last year Mark grew 4 cm taller. Now he is 1 cm shorter than the table. How many cm was Mark shorter than the table before?)

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