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Volume 1**

**Editors
Anne D Cockburn
Elena Nardi**



**School of Education and Professional Development
University of East Anglia**

*Proceedings of the 26th Conference of the International group for the Psychology of
Mathematics Education*

Volume 1

Editors

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Welcome to PME 26

Welcome to PME 26! The School of Education and Professional Development at the University of East Anglia is delighted to be hosting the twenty-sixth annual meeting of the International Group for the Psychology of Mathematics Education. The theme for the conference this year is 'Learning from Learners' which, we are pleased to report, has captured the imagination of many of this year's contributors. In total we have in the region of 290 presentations, ranging from the psychology of mathematics in the very early years to discussions on advanced mathematical concepts. We will also be offering you a variety of entertainment that will restore your energy levels amid the demands of such a busy scientific programme.

We very much hope you enjoy your stay in Norwich and that you will feel welcome to return in years to come. The city dates back to Anglo-Saxon times and offers a wealth of sights, including a Norman castle (1067), two magnificent cathedrals (1096 and 1894) and what the eighteenth century historian, Francis Bloomfield, described as the 'grandest market in all England'. We recommend that you take the opportunity to wander around the city and discover its delights for yourself.

We hope that the conference will run smoothly with, apparently, very little effort on our part. If it doesn't, I can only reassure you that we have done, and will do, our very best! If it does all go well it will be due to many months of preparation and commitment from numerous people. We thank them all, especially members of the Local and Programme Committees. Particular attention must go to Gilah Leder for her encouragement in the early days of our work and to Rina Hershkowitz for continuing such support. Thanks too to Janet Ainley who proved to be an excellent Chair for the Programme Committee. The invaluable help of Lucila Recart and Bella Radford was also much appreciated. Angela Hook's and Claire Butler's hard work should not go unmentioned either. Joop van Dormolen's ceaseless labours in both creating and refining the computer programme we relied on and his endless patience and enthusiasm also deserve particular recognition. And finally, a special mention to Elena Nardi, without whom this venture would have been impossible.

More formally, we would like to thank the following sponsors:

- The Lord Mayor of Norwich for his most generous contribution on our arrival at the dinner dance;
- Jarrolds Department Store for heavily subsidising the Norwich guidebooks in your conference pack;
- Falmer Press for providing conference pens;
- Paul Chapman Publishers for donating conference notebooks;
- Colmans of Norwich for the savoury packs in your conference bag;
- The University of East Anglia for providing us with both time and space to host this conference.

Finally, should you have any questions/concerns during your stay, please do not hesitate to ask members of the conference team. We very much hope that you enjoy PME 26 and that you return home feeling refreshed and invigorated.

With very best wishes,

Anne Cockburn
on behalf of the PME 26 Conference Committees

Summer 2002

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