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**Editors
Neil A. Pateman
Barbara J. Dougherty
Joseph T. Zilliox**

**CRDG, College of Education,
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Volume 3

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